High-Resolution Diffusion-Weighted Imaging With Interleaved Variable-Density Spiral Acquisitions

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Purpose: To develop a multishot magnetic resonance imaging (MRI) pulse sequence and reconstruction algorithm for diffusion-weighted imaging (DWI) in the brain with submillimeter in-plane resolution.

Materials and Methods: A self-navigated multishot acquisition technique based on variable-density spiral k-space trajectory design was implemented on clinical MRI scanners. The image reconstruction algorithm takes advantage of the oversampling of the center k-space and uses the densely sampled central portion of the k-space data for both imaging reconstruction and motion correction. The developed DWI technique was tested in an agar gel phantom and three healthy volunteers.

Results: Motions result in phase and k-space shifts in the DWI data acquired using multishot spiral acquisitions. With the two-dimensional self-navigator correction, diffusion-weighted images with a resolution of 0.9 x 0.9 x 3 mm3 were successfully obtained using different interleaves ranging from 8 – 32. The measured apparent diffusion coefficient (ADC) in the homogenous gel phantom was (1.66 ± 0.09) x 10-3 mm2/second, which was the same as measured with single-shot methods. The intersubject average ADC from the brain parenchyma of normal adults was (0.91 ± 0.01) x 10-3 mm2/second, which was in a good agreement with the reported literature values.

Conclusion: The self-navigated multishot variable-density spiral acquisition provides a time-efficient approach to acquire high-resolution diffusion-weighted images on a clinical scanner. The reconstruction algorithm based on motion correction in the k-space data is robust, and measured ADC values are accurate and reproducible.

Key Words: diffusion-weighted imaging; self-navigator; motion correction; interleaved variable-density spiral acquisition; high-resolution MRI


THE CLINICAL UTILITY OF DIFFUSION-weighted imaging (DWI) for rapid assessment of acute stroke (1) has been well established. The extension of DWI into diffusion tensor imaging (DTI) to explore the diffusion anisotropy has recently become a promising technique for noninvasive mapping of neuronal connectivity in the living human brain (2–5). This technique is also very useful for detecting abnormalities in white matter integrity, composition, and development caused by neurological and psychiatric disorders (5,6). However, the potential of this technique to study complex and detailed cerebral connectivity is greatly limited by the low spatial resolution and poor signal-to-noise ratio (SNR) of the most commonly used single-shot imaging techniques. Improving the spatial resolution and SNR of DWI is of great importance for the detailed mapping of the complex neuronal pathways in the brain with DTI. The lack of spatial resolution and SNR also pose severe limitations for its clinical applications, because it is difficult to detect minor structural changes in the white matter associated with brain disorders.

The limited spatial resolution of diffusion-weighted images is inherently associated with the severe motion sensitivity of DWI. The large displacement encoding gradient pulses applied in DWI measurements are not only sensitive to the microscopic random molecular motions, but also very sensitive to the physiological motions in the brain, such as cardiac and respiratory-driven pulsations, cerebral spinal fluid (CSF) flow, and involuntary body movements. Neither can the effect of vibration induced by the strong diffusion-weighting gradients be ignored, as evidenced by the severe artifacts observed in DWI of gel phantoms. DWI pulse sequences descend from single-shot magnetic resonance imaging (MRI) techniques, such as echo-planar imaging (EPI) (1,6,7), spiral imaging (8–10), and fast spin echo (FSE) (11,12), are less prone to motion arti-

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between interleaves can result in nonuniform sampling of k-space and render the diffusion-weighted images with severe motion artifacts (19). In the present study, we implemented a variable-density spiral trajectory design to adequately oversample the inner k-space portion (the first 100 data points of each interleave covering less than 0.5% of the k-space radius). With this design, the motion-induced phase shift and k-space offset between interleaves can be reliably estimated from multiple data points in a least-squares sense. Another advantage of this method is that the trajectory can be calculated using a simplified analytical solution (8,20), which enables flexible prescription of the scanning parameters.

**MATERIALS AND METHODS**

The proposed imaging method includes three steps: 1) variable-density spiral data acquisition, 2) self-navigated motion correction, and 3) imaging reconstruction. The details for each step are discussed below.

**Design of the Variable-Density Spiral Trajectory**

The design of the variable-density trajectory is usually accomplished by feeding the desired sampling density profile into a gradient waveform design algorithm. In the present study, the spiral trajectory was designed using the following empirical approximation:

$$k(t) = (N/2/\text{FOV})^n \exp (i2\pi nt)$$  \hspace{1cm} (1)

where N and FOV are the matrix size and field of view of the image, respectively. $\alpha$ is an empirical parameter that determines the degree of oversampling near the origin and is typically in the range of $\alpha \approx (2,6)$. $n$ is the number of turns in the k-space trajectory.

A typical spiral trajectory will start off in the slew-rate-limited region. After reaching its maximum gradient amplitude, it will switch to the amplitude-limited region. Following the piecewise approximation approach proposed by Glover (8,20), the above variable-density spiral trajectory can be analytically calculated using the following equations:

$$\tau(t) = \begin{cases} \left[ \frac{\gamma g_m}{\lambda \omega} \left( \alpha/2 + 1 \right) \right]^{1/(1 + \alpha/2)} & 0 \leq t \leq t_c \\ \left[ \frac{\gamma g_m}{\lambda \omega} \left( 1 + \alpha \right) \right]^{1/(1 + \alpha)} & t_c \leq t \leq t_{\text{end}} \end{cases}$$

(2)

where $g_m$ and $s_m$ are the maximum gradient amplitude and maximum gradient slew rate, respectively. $\lambda = N/\text{FOV}$, $\omega = 2\pi n$, $\gamma$ is the proton gyromagnetic ratio, and $t_c$ represents the time point when the trajectory changes from a slew-rate-limited regime to an amplitude-limited regime. A detailed analysis of the design has been given elsewhere (20). It is worthwhile to point out that the $\alpha$ parameter determines the extent of oversampling near the k-space origin. For example, when $\alpha = 1$, this will be a constant-density trajectory as described in Glover (8). Larger values of $\alpha$ will result in a higher degree of oversampling at the cost of off-reso-
nance effects due to a longer readout. Figure 2 illustrates this by plotting the sampling point within the center 0.5% of the k-space trajectory for a 256 × 256 acquisition over an FOV = 230 mm using 16 interleaves. In this study, α = 4 was used to achieve adequate oversampling for robust motion corrections.

The acquisitions of different interleaves were implemented by taking advantage of the rotation matrix subroutine for the gradient waveforms. Once the readout gradient waveforms for the unrotated first interleave were computed as described above, the readout gradient waveforms for the other interleaves were obtained at the run time from the unrotated gradient waveforms by multiplying with the corresponding rotation matrices. The rotation angle for the i-th interleave for a design with a total of m interleaves is equal to $2\pi m (i - 1)$, where $1 \leq i \leq m$.

**Self-Navigated Motion Correction**

Motions during the application of diffusion-weighting gradients result in three-dimensional k-space displacements, which are difficult to be theoretically predicted. Both the phase shifts and k-space offsets need to be measured and compensated for individual interleaves before combining the data to construct a high-resolution diffusion-weighted image. It is necessary to implement at least a two-dimensional navigator motion correction mechanism for acquiring diffusion-weighted images with multishot acquisitions. This is accomplished by using the oversampled initial portion of each spiral readout as a self-navigator.

To estimate the motion-induced phase shift and k-space displacement of the data, a least-squares fitting algorithm was implemented by fitting a two-dimensional sinc function to the adequately oversampled portion of the k-space modulus data. The k-space coordinate offsets from the origin and phase of the peak signal were assigned as the k-space displacement and phase shift of the signal, respectively. We also tested the method used by Butts et al (7), in which a signal intensity-weighted average phase value was estimated based on the points located within the main lobe of the k-space data. The results from the later method were somewhat dependent on the weighting method and the intensity threshold used to select the data points.

The correction of the k-space displacement was performed by using the actual in-plane k-space trajectory in the gridding procedure. In the absence of motion, the designed center k-space path should coincide from view to view in multishot spiral acquisitions. With motions, the actual k-space trajectory should be the designed trajectory plus the estimated deviations. Gridding with the actual k-space path can therefore compensate the effects of motions. Out-of-plane motions can result in k-space offsets in the third dimension. To mitigate the out-of-plane motion artifacts using a two-dimensional in-plane navigator mechanism, a provisional measure was implemented, which excludes an entire interleave when the signal is so corrupted that its intensity is less than 70% of the maximum of all interleaves.

**Image Reconstruction**

When the k-space data do not fall on the Cartesian linear grid, as is the case with spiral trajectory in addition to the arbitrary motion-induced deviations, gridding interpolation is one of the most widely used image reconstruction methods. The gridding interpolation was performed off-line on a Sun workstation using the method described by Meyer et al (16). To compensate for the nonuniform k-space sampling density of the data acquisition, a nonlinear weighting was applied to the raw data. The compensation function used here was based on the absolute value of the Jacobian determinant in the transformation to Cartesian coordinates from the spiral trajectory, along which data were actu-
ally acquired (10). The actual k-space path was calculated as the sum of designed trajectory and the estimated deviation from the self-navigator. The convolution kernel for gridding was a two-dimensional Kaiser-Bessel function with a fixed width of 1.5/FOV to convolve the raw data sampled in spiral trajectories onto a two-dimensional doubly oversampled square matrix.

After applying a window function that matches the designed variable-density spiral profile, a two-dimensional fast Fourier transformation (FFT) was performed to produce the image in real space. When the applied window function is proportional to the sampling density, the general theory of variable-density sampling illustrates that the side lobes in the point-spread function can be reduced without an increase in the noise variance (21). It should be noted that the sampling radius has to be doubled to preserve the same SNR and resolution when the window function is applied. This is also the case for uniform spiral design. Before the computation of the amplitude image, the complex image was rescaled by the Fourier transformation of the gridding kernel to correct the image intensity modulation caused by the convolution. Our reconstruction routine also used a $B_0$ field map acquired at the beginning of the diffusion acquisition to correct for linear shim terms and carrier frequency offsets in each slice.

**Experimental**

The diffusion-weighted MRI pulse sequence with variable-density spiral trajectory was implemented on GE Signa 1.5-T and 3-T whole-body MRI scanners using the EPIC LX 9.0 platform. Since both scanners were equipped with the same gradient hardware, which can provide the maximum gradient strength of 40 mT/m and the slew rate of 200 T/m/second, the implementation was transparent on both systems and the scanning protocols were also the same. For comparison, with a given acquisition prescription, the sequence has the option to choose either a variable- or constant-density spiral trajectory. The sequence was first tested using an agar gel phantom at $b = 600$ seconds/mm$^2$ and a matrix size of $256 \times 256$. The tests included image quality and diffusion coefficient reproducibility using different number of spiral interleaves. In vivo measurements were then performed in three male volunteers (aged between 32 and 38 years old) using the following protocol: $b = 1000$ seconds/mm$^2$, matrix size = $256 \times 256$, FOV = $230$ mm, slice thickness = $3$ mm, NEX = 1, TE/TR = $80/6000$ msec, acquisition bandwidth = $100$ kHz, and four different diffusion-weighting directions (xyz, $-x-y+z$, $x-y-z$, $-x+y-z$). For quantification of the apparent diffusion coefficient (ADC), the average result from the four diffusion-weighting gradient directions was used. It has been shown (22) that the average is proportional to the trace value of the diffusion tensor and independent of the direction of the diffusion-weighting gradient. The maximum available gradient strength was used for each diffusion-weighting gradient with $\delta = 35.1$ msec and $\Delta = 35.5$ msec. Three different designs based on 8, 16, and 32 interleaves were used for the spiral readout gradient waveforms. The durations of the readout gradient for uniform and variable-density acquisitions are listed in Table 1. Although the radius of k-space coverage for the uniform and variable-density spiral was about the same, the readout duration for the variable-density spiral was 50% to 70% longer due to the oversampling in the center. Each subject completed six sets of DWI measurements using three different interleaves combined with uniform and variable-density spiral waveforms on both 1.5-T and 3-T scanners. Three repeated measurements were performed for each set of data acquisition parameters. The experiment on each scanner lasted for about 2 1/2 hours for each subject.

**RESULTS**

As shown in Fig. 3, motions in DWI measurements can give rise to signal distortions in different fashions ranging from signal loss to k-space offset. With the two-dimensional self-navigator, the in-plane k-space offset can be reliably measured and corrected. As shown in Fig. 4, the k-space offsets for the majority of interleaves are in the range of $\Delta k = \pm 3$/FOV. The radius and density of the oversampled self-navigator at $\alpha = 4$ are apparently adequate for reliable estimate of the k-space offsets associated with low to moderate degrees of motions during the application of diffusion-weighting gradients.

With the constant-density spiral trajectory, the diffusion-weighted MR images collected from the human brains (Fig. 5a and c) have severe motion artifacts. For this design, the motion correction navigator based on the phase error estimates from the first two data points in each interleave can reduce the motion artifacts somewhat. This is apparently not robust, as illustrated by comparing images in Fig. 5a with those in Fig. 5c. The interleaved spiral acquisitions with constant density cannot reliably measure ADC in the phantom and human brains. The variations between individual measurements were larger than 30%. With the variable-density trajectory design, the image quality of the diffusion-weighted image was improved even without implementing any motion correction scheme (Fig. 5b). As shown in Figs. 5d and 6, using a more robust motion correction method can progressively improve the image quality and SNR to a higher level. The average ADC $\pm$ SD for each data set collected using variable-density gradient waveforms at 3 T is summarized in Table 2. The SD for the in vivo measurements for individual

<table>
<thead>
<tr>
<th>Interleaves (N)</th>
<th>Interleave (uniform)$^a$</th>
<th>Duration (msec)$^b$</th>
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</thead>
<tbody>
<tr>
<td>8</td>
<td>26.74</td>
<td>46.30</td>
</tr>
<tr>
<td>16</td>
<td>13.52</td>
<td>22.40</td>
</tr>
<tr>
<td>32</td>
<td>6.98</td>
<td>10.45</td>
</tr>
</tbody>
</table>

$^a$For the case of $\alpha = 1$.

$^b$For the case of $\alpha = 4$. 

Table 1
The Length of Spiral Readout to 8, 16, and 32 Interleave ($^m$)
subjects was about 8%, which is somewhat higher than the 5% for the phantom data. The average ADC measured in the homogenous gel phantom was \( (1.66 \pm 0.09) \times 10^{-3} \text{ mm}^2/\text{second} \), which was identical to what was measured with single-shot methods.

The images shown in Fig. 5d were acquired at 1.5 T using 16 interleaves. Figure 6 shows a typical set of images acquired at 3 T using 32 interleaves. As shown, shortening the readout duration in each interleave by increasing the number of interleaves reduces the local off-resonance effect (blurring). The average interindividual ADC in the normal brain tissue estimated from such measurement was \( (0.91 \pm 0.01) \times 10^{-3} \text{ mm}^2/\text{second} \), which is consistent with the literature values (1,7,10,12).

**DISCUSSION**

The variable-density spiral acquisition sequence is well suited for DWI because the inherent robustness of central out acquisition methods to motion artifacts (9). This is also attributable in part to oversampling of central k-space, which reduces artifacts in a similar manner as signal averaging with multiple acquisitions. Furthermore, starting data sampling from the origin of k-space greatly reduces the moment of imaging gradient in the central k-space and motion-induced image phase error (type II artifacts) (9,23). The advantages for implementing a simplified variable-density spiral trajectory design using a closed-form approximation for DWI are the following: 1) robust motion correction mechanism based on self-navigator signal, 2) high efficiency of data acquisition for high-resolution DWI, and 3) flexible applicability for different protocols and hardware. The main limitation, however, is that it cannot reliably correct the effect of through-plane motions, as in all other two-dimensional acquisition methods. The out-of-plane motion can cause significant signal reduction, and this
can be particularly problematic in brain regions where cardiac and respiratory pulsations are most active. The data rejection based on signal peak intensity removes the worst affected interleaves, but it does not correct the remaining interleaves on the phase errors associated with out-of-plane motions.

It was recently suggested that motion correction in the imaging space might be needed to correct for nonlinear phase effects (12,19,24). One necessary condition to perform image space phase correction is that a complete image must be constructed from each interleave of the multishot acquisition. Depending on the acquisition strategy, the image constructed from a subset of the complete data set can exhibit either blurring or aliasing. For example, if each subset is densely sampled ($\Delta k = 1/\text{FOV}$), with a rotating band passing the center of k-space as in the PROPELLER sequence (12), the constructed image will be simply blurred with limited resolution and the phase correction in the image space can be adequately done after removing the ringing. If each subset covers the entire k-space but does not sample as sufficiently dense as the variable-density spiral scans used here, the signal will be averaged globally and the constructed image from a single interleave generally contains aliased high-frequency artifacts. In this case, the image-based correction cannot be done correctly and the correction algorithm based on k-space data is more adequate. It is possible to construct an image of very low resolution from each spiral interleave based on the oversampled portion of the data. However, this would require a significant portion of each interleave to be densely sampled.

Given the limited imaging time available in clinical situations such as acute stroke, time efficiency is a very relevant issue for DWI sequence development. The interleaved variable-density spiral method is extremely time efficient; whole-brain diffusion-weighted image data set up to 50 slices can be acquired within three minutes using a TR of five seconds and 32 interleaves. Time efficiency is also essential for DTI and Q-space imaging, which require multiple diffusion-weighting directions and b-values. In most clinical stroke studies (1,10), ADC measurements were typically conducted using two points of different b-values. When image degradation due to increased sensitivity to motion artifacts and susceptibility artifacts is not considered (25), the optimum SNR in ADC is obtained by choosing $b = 1.1/\text{ADC}$. For normal brain tissues, this requires a b-value of about 1000 seconds/mm$^2$, as used for the in vivo measurements in this work. The formation of average ADC maps from multiple measurements using an appropriate distributed gradient set (26) may help improve SNR and remove the effects of white matter anisotropy desirable for clinical diagnostics.

Improving the spatial resolution, reducing imaging artifacts, and optimizing SNR for DWI are important issues both for clinical application and for detailed mapping of the complex neuronal pathways in the brain. As such, the development of new techniques and strategies for motion correction in the imaging space becomes increasingly important in order to further improve the quality and accuracy of diffusion imaging studies.

**Figure 5.** Comparison of diffusion-weighted images (FOV = 230 mm, matrix size = 256 × 256) acquired in the transverse plane using 16 interleaved spiral readouts with the constant- [a and c] and variable- [b and d] density trajectory designs. Without implementation of self-navigated motion correction, motion artifacts render the images useless (a and b). The motion artifacts in the images (c and d) are reduced by applying even a simple motion correction mechanism based on the first two data points in each interleave. The four different images in each row were acquired using four different diffusion-weighting gradient directions (the tetrahedral set: xyz, –x–y+z, x–y–z, –x+y–z), respectively.
brain with DTI. For example, very small lesions of 1–2 mm in size could be missed or blurred out in low-resolution images based on single-shot techniques (7,12). The limited spatial resolution and SNR also pose a severe problem for clinical applications of DTI, because minor structural changes in the white matter associated with neuropsychiatric disorders cannot be reliably detected with single-shot techniques (5). For future development, we will combine this multishot variable-density spiral sequence for DWI with some optimized DTI schemes (26) for high-resolution DTI studies.

In conclusion, the preliminary results from this study demonstrate that self-navigated multishot DWI based on the variable-density spiral trajectory design is adequately robust to acquire high-resolution diffusion-weighted images without the need of excessive head restraint and cardiac gating. This acquisition method oversamples the central k-space densely in each interleave and allows for self-navigated motion correction. Further enhancement of the robustness against motion artifacts can be achieved by exclusion of corrupted data acquisition due to out-of-plane or excessive in-plane motions. When the motion artifact problem in DWI is solved, the multishot DWI technique has significant advantages, such as good spatial resolution and reduced magnetic susceptibility artifacts. The implementation of this time-efficient k-space sampling method is highly simplified by using the closed-form approximation for on-line waveform calculation. The solution remains well behaved in the both gradient slew-rate- and amplitude-limited regions. The ability to calculate readout waveforms using an analytical formula provides flexibility to test scanning protocols and hardware characteristics.

Figure 6. The isotropic diffusion-weighted images (a) at $b = 1000$ seconds/mm$^2$ acquired using 32 interleaves of variable-density spiral method and the corresponding ADC maps (b). The following acquisition parameters were used: $B_0 = 3$ T, TE/TR = 80/6000 msec, FOV = 230 mm, matrix size = 256 × 256, and slice thickness = 3 mm. Both the diffusion-weighted images (a) and ADC maps (b) are the average results from the measurements using the tetrahedral gradient set and are equivalent to the average results from an infinite number of diffusion-weighting directions.
Table 2
The Average ADC ± SD in 10⁻³ mm²/seconds for the Phantom and Individual Subjects*

<table>
<thead>
<tr>
<th></th>
<th>N = 8</th>
<th>N = 16</th>
<th>N = 32</th>
</tr>
</thead>
<tbody>
<tr>
<td>Gel phantom</td>
<td>1.67 ± 0.09</td>
<td>1.65 ± 0.09</td>
<td>1.66 ± 0.08</td>
</tr>
<tr>
<td>Subject 1a</td>
<td>0.90 ± 0.07</td>
<td>0.92 ± 0.07</td>
<td>0.91 ± 0.06</td>
</tr>
<tr>
<td>Subject 2a</td>
<td>0.93 ± 0.07</td>
<td>0.93 ± 0.08</td>
<td>0.92 ± 0.07</td>
</tr>
<tr>
<td>Subject 3a</td>
<td>0.92 ± 0.09</td>
<td>0.91 ± 0.07</td>
<td>0.90 ± 0.06</td>
</tr>
<tr>
<td>Intersubject</td>
<td>0.92 ± 0.02</td>
<td>0.92 ± 0.02</td>
<td>0.91 ± 0.01</td>
</tr>
</tbody>
</table>

*aThe in vivo ADC results were evaluated from at least six brain ROIs carefully selected to void cerebral spinal fluid.

REFERENCES